

The research on banknote authenticity discrimination analysis algorithm based on wavelet transform features

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Abstract: In the authenticity identification of banknotes, features such as variance, skewness, kurtosis, and entropy of the images transformed by wavelet are used. This paper combines distance discriminant analysis, Fisher discriminant analysis, and Bayesian discriminant analysis for discrimination analysis. Variance can measure the texture complexity and grayscale level variation in the image, skewness is used to evaluate the symmetry and deviation from the normal distribution of the image, and kurtosis can measure the texture structure and grayscale level concentration. The entropy of the image reflects the complexity and uncertainty of the image. These features can be used to distinguish genuine banknotes from counterfeit ones.

1. Introduction

Background The authenticity identification of banknotes has always been an important research direction in the fields of finance and public security. With the development of technology, image processing and pattern recognition techniques have been widely applied in banknote authenticity identification. The classification analysis based on image features after wavelet transform and distance discrimination method, Fisher discrimination method, and Bayesian discrimination method have become hot research topics.

In terms of research background, the following aspects can be discussed:

1) The importance and application scenarios of banknote authenticity identification: The importance of banknote identification in the field of finance and public security cannot be underestimated, as well as its practical application scenarios in daily life, such as self-service vending machines, ATMs.

2) Currently the mainstream authenticity of the method: identify the authenticity of banknotes are mainly two methods of infrared detection. Infrared radiation scans the banknote to recognize the unique infrared spectral characteristics of the banknote. Ultraviolet detection through ultraviolet light irradiation of banknotes, observe its fluorescence in the ultraviolet light reaction, so as to determine the authenticity [1].

3) Application of image processing and pattern recognition in banknote authenticity identification: The application of image processing and pattern recognition techniques in banknote authenticity identification includes image preprocessing, feature extraction, and classifier design.

4) Application of wavelet transform in image processing: Wavelet transform is a powerful mathematical tool that is widely used in image processing. The basic principle is to decompose the image into subbands of different frequencies by a set of wavelet functions [2].

5) Discriminant analysis works well for classification problems. Discriminant analysis is a statistical method mainly used for classification and pattern recognition problems. The core idea is to correctly classify a new sample into its own category by analyzing the features of different categories [3].

Through the explanation of the research background, the reader can understand the importance of identifying the authenticity of banknotes and the value of the application of the ripplelet transform and classification methods in this field by explaining the background of the study. It is understood that discriminant analysis is used in classification problems and identifying the authenticity of banknotes is also a binary classification problem. This information guides the selection of the content of the subsequent research and the selection of the research methodology.

The study compiles data sourced from Kaggle datasets, amassing a total of 1096 data points. Following data collection, initial processing procedures are executed. Evaluating the accuracy of banknote classification involves utilizing diverse methodologies like distance variance, Fisher's technique, and Bayesian discriminant analysis across the gathered dataset. The findings from these approaches are subjected to a lot of analysis and integration to provide final conclusions. Going by these facts, the recommendations and solutions given are accurately formulated.

2. Research objectives and significant

2.1 Objectives

This chapter intends to employ the distance judgment, the Fisher judgment, and the Bayesian judgment in order to increase the efficiency and the correctness of distinguishing the forged banknotes from the genuine ones. The objective is to determine the effectiveness of wavelet transformed images' features, including variability, asymmetry, shape, and randomness, to verify the genuineness of currency notes in order to select the most efficient method of verification.

This paper's primary objective is to improve the accuracy of banknote identification with the help of better techniques. Hence, through analysis of real and counterfeit currency, a fast and efficient mechanism to differentiate between the two has been established. This innovation, therefore, opens a new chapter in currency verification technology, and eliminates the occurrence of fake currency

transactions in practical use thus enhancing the credibility of the financial systems.

In summary, this paper seeks to design efficient, precise and reliable systems for the identification of banknotes using different analytical methods and specific characteristics of the currency. These are important in enhancing the stability of financial systems and encouraging lasting development of the economy.

2.2 Significance

One of the main issues in today's society is the efficient identification of forged banknotes as soon as possible. The use of fake currency is a huge menace to the economy due to the fact that it threatens the safety and stability of monetary exchanges within the population.

Small amounts of counterfeit money need to be detected reliably so that it will not continue circulating within the financial system to compromise the financial system.

For the consumers to be safe against counterfeit notes, fake money has to be detected to promote the general well-being of the consumers, legit transactions and the confidence levels of the consumers.

To enhance the facets of market quality, then the process of identifying counterfeit notes has to be streamlined to improve market efficiency and encourage reliable and fair business interactions.

These measures not only minimize economic effects in terms of circulation of counterfeit notes, but also enhance the solidity of financial organizations as well as contribute to the growth of society's and the economy's wellbeing.

3. Data description

Data Source: The data for this study is obtained from the Kaggle database, specifically from the following link: "<https://www.kaggle.com/datasets/gauravduttakiit/banknote>".

Variable Descriptions:

X1: VWTI - Variance of Wavelet Transformed Image

X2: SWTI - Skewness of Wavelet Transformed Image

X3: CWTI - Curtosis of Wavelet Transformed Image

X4: EI - Entropy of Image

Class: There are two classes, 0 and 1. Class 1 represents genuine banknotes and class 0 represents counterfeit banknotes.

4. Empirical analysis

Data Processing: First, the 1096 sample data were processed. Upon observation, counterfeit bank data it can be seen that the data has already been categorized in the table. The category "0" represents counterfeit bank data and the category "1" represents genuine banknotes. Among the samples, there are 608 classified as counterfeit bank data and 488 classified as genuine banknotes. We selected 608 counterfeit bank data data samples as class one, 292 genuine banknote data samples as class two, and 196 genuine banknote data samples for predicting classification effectiveness.

4.1 Model 1

Mahalanobis distance is a distance measurement method that takes into account the covariance structure between samples. It is used to measure the distance of a sample point relative to the mean vector of a given category in a multi-dimensional space [3].

Based on the theoretical basis mentioned above, the code follows these steps:

Check and process the input parameters. If the test sample is not provided, the training samples classG1 and classG2 are combined as the test sample by default.

Calculate the number of rows in the test sample and initialize the classification result matrix.

Calculate the mean vectors for the training samples respectively.

If var.equal is TRUE or T, the covariance matrix for the combined samples is computed assuming equal variances. Use the Mahalanobis distance function to compute the Mahalanobis distance of the test samples relative to the sample category mean vector, and then subtract the two to obtain the discriminant function value. If var.equal is FALSE, the covariance matrices of the two categories are computed separately, assuming unequal variances. The Mahalanobis distance function is used to calculate the Mahalanobis distance of the test sample with respect to the mean vector of the sample categories, and then they are subtracted to obtain the value of the discriminant function.

Iterate the discriminant function values, classify the test samples into 0 or 1 classes according to specific conditions and store the results in the classification result matrix. Return the classification result matrix.

In summary, these steps are based on the theoretical foundations of discriminant analysis and implement a discriminant analysis function. It is used to classify and predict given training and test samples.

	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27
blong	0	0	1	0	0	0	1	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0
	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51			
blong	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	52	53	54	55	56	57	58	59	60	61	62	63	64	65	66	67	68	69	70	71	72	73	74	75			
blong	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	76	77	78	79	80	81	82	83	84	85	86	87	88	89	90	91	92	93	94	95	96	97	98	99			
blong	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	100	101	102	103	104	105	106	107	108	109	110	111	112	113	114	115	116	117									
blong	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0
	118	119	120	121	122	123	124	125	126	127	128	129	130	131	132	133	134	135									
blong	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	136	137	138	139	140	141	142	143	144	145	146	147	148	149	150	151	152	153									
blong	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	154	155	156	157	158	159	160	161	162	163	164	165	166	167	168	169	170	171									
blong	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	172	173	174	175	176	177	178	179	180	181	182	183	184	185	186	187	188	189									
blong	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	190	191	192	193	194	195	196	197	198	199	200	201	202	203	204	205	206	207									
blong	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	208	209	210	211	212	213	214	215	216	217	218	219	220	221	222	223	224	225									
blong	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	226	227	228	229	230	231	232	233	234	235	236	237	238	239	240	241	242	243									
blong	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	244	245	246	247	248	249	250	251	252	253	254	255	256	257	258	259	260	261									
blong	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	262	263	264	265	266	267	268	269	270	271	272	273	274	275	276	277	278	279									
blong	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	280	281	282	283	284	285	286	287	288	289	290	291	292	293	294	295	296	297									
blong	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	298	299	300	301	302	303	304	305	306	307	308	309	310	311	312	313	314	315									
blong	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1
	316	317	318	319	320	321	322	323	324	325	326	327	328	329	330	331	332	333									
blong	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	334	335	336	337	338	339	340	341	342	343	344	345	346	347	348	349	350	351									
blong	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	352	353	354	355	356	357	358	359	360	361	362	363	364	365	366	367	368	369									
blong	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1

Figure 1. Partial presentation of classification results

The Figure 1 show that only counterfeit bills with serial numbers 3, 7, 15, 116, 240, 315, 347, 368, and the undisplayed 407, 454 were misclassified as genuine bills. It can be seen that out of 900 samples, only 10 were misclassified, resulting in a discrimination accuracy was approximately 98.89%. Finally, the prediction accuracy of the test set is obtained as 100% by running it through the R language

4.2 Model 2

The specific summary of the Fisher’s discriminant method is as follows:

By using the attach (data) function, the variables in the dataset ‘data’ are loaded into the environment so that they can be directly operated using variable names.

The library (MASS) is used to load the MASS package in R, which provides functions for performing LDA.

A LDA model is created by calling the lda() function. The formula Class~X1+X2+X3+X4 specifies the model, indicating that the target variable is Class and the predictor variables are X1, X2, X3, and X4. Data [1:900,] represents using the first 900 samples in the dataset as training data.

The generated LDA model is assigned to the variable ld, so that it can be used for prediction or other operations later. The output result is as follows:

Table 1: LDA model output results

	Groups	Prior Probabilities	X1	X2	X3	X4
	0	0.6755556	2.322898	4.154896	0.8369718	-1.092019
	1	0.3244444	-1.987436	-1.259352	2.5025157	-1.317595
coefficients			-0.832242506	-0.447299820	-0.592249084	0.008778945

In Table 1, we have two classes labeled as 0 and 1. In the first 900 samples of the dataset, the prior probability of class 0 is 0.6755556, and the prior probability of class 1 is 0.3244444. The model also provides the mean vectors for each class. For class 0, the mean of X1 is 2.322898, the mean of X2 is 4.154896, the mean of X3 is 0.8369718, and the mean of X4 is -1.092019. For class 1, the mean of X1 is -1.987436, the mean of X2 is -1.259352, the mean of X3 is 2.5025157, and the mean of X4 is -1.317595. Lastly, the model provides the coefficients of the linear discriminant function. Based on these coefficients, a new data point can be classified using the linear discriminant function. For the linear discriminant function, the coefficients for the discriminant variable LD1 are -0.832242506 (X1), -0.447299820 (X2), -0.592249084 (X3), and -0.008778945 (X4).

Table 2: Confusion Matrix

New G	Class_0	Class_1
0	585	23
1	0	292

Table 3: Test set prediction posterior probability

NO.	0	1
31	5.009199e-06	0.9999950
32	3.974186e-05	0.9999603
33	5.087928e-01	0.4912072
34	9.918076e-08	0.9999999

According to the Table 2, the Fisher discriminant yields a backward judgment prediction rate of 97.44%. According to the Table 3. The posterior probability of data point #33 is 0.4912072, which suggests that in the new data prediction, this data point is more likely to belong to categorization 0 than to categorization 1. So NO. 33 is misclassified, resulting in a discrimination prediction accuracy was approximately 99.49%.

4.3 Model 3

The third model is the naive Bayesian classifier, which is a probabilistic classification method based on Bayes' theorem and is often considered a type of Bayesian discriminant method [3]. The code uses naiveBayes function to fit a plain Bayesian model where Class variable is the response variable and X1, X2, X3 and X4 are the predictor variables. The model formula $Class \sim X1 + X2 + X3 + X4$ is used to build the classifier. In modeling, the code uses only the first 900 rows of the dataset (data [1:900,]). The code classifies the data through a plain Bayesian approach and generates an object nb containing the model parameters and results.

Table 4: A priori probability distribution

Y	Probability
0	0.6755556
1	0.3244444

The Table 4 displays some important information about the prior probabilities of the classes in the dataset used to train the Naive Bayes classifier. Specifically, it shows the likelihood of an instance belonging to each class before considering any of the feature values.

From the table we can infer that the probability that an instance belongs to class 0 ($Y = 0$) is 67.56%, which indicates that class 0 is more common in the dataset. The probability that an instance belongs to class 1 ($Y = 1$) is 32.44%, which indicates that class 1 is less common in the dataset. For the Naive Bayes classification process, these probabilities are key starting points because they represent the base rate for each category, regardless of the effect of predictor variables. Understanding these baseline probabilities helps to properly understand the classifier output and make informed decisions based on the model predictions.

Table 5: Confusion Matrix

New G	Class_0	Class_1
0	552	56
1	78	214

According to Table 5, 552 instances with actual category 0 were correctly predicted to be 0 and 56 were incorrectly predicted to be 1. Of the instances with actual category 1, 214 were correctly predicted to be 1 and 78 were incorrectly predicted to be 0. Overall, the model's accuracy was 85.11%. Finally, according to the output of the program, 60 samples were misclassified, so the prediction accuracy is approximately 69.39%.

5. Conclusion and recommendations

5.1 Conclusion

Based on the research on counterfeit banknote detection, this paper comprehensively utilizes distance discrimination, Fisher discrimination, and Bayesian discrimination methods, and analyzes the features of variance, skewness, kurtosis, and entropy of wavelet transformed images. The empirical results show that among these features, the Mahalanobis distance discrimination method performs better in counterfeit banknote detection.

Variance measures texture complexity and gray-level variation, skewness evaluates symmetry and deviation from normal distribution, and kurtosis measures texture structure and gray-level distribution aggregation. Entropy reflects complexity and uncertainty. Comprehensive use can distinguish genuine and counterfeit banknotes.

The above features are significant in the detection of counterfeit banknotes. Empirical results show that the Mahalanobis distance discrimination method performs better than the other two methods. The selection of the appropriate discrimination method should be based on specific application scenarios, combined with the characteristics of the data set to consider. In practical application, the advantages and disadvantages of various discrimination methods should be comprehensively evaluated and reasonably selected, so as to achieve more reliable detection of counterfeit coins.

5.2 Recommendations

From the empirical results, the Mahalanobis distance discrimination method performs better in the detection of counterfeit banknotes. In practical applications, it is recommended to give priority to Mahalanobis distance discrimination method in detecting counterfeit banknotes. Further research to improve the counterfeit currency detection method, can consider the introduction of texture features and other features to improve the accuracy of counterfeit currency detection. The detection efficiency of counterfeit banknotes can be further improved by adopting emerging technologies such as deep learning. In order to ensure the reliability and robustness of the detection system to adapt to the evolving technology of banknote manufacturing, it is necessary to expand and update the data set.

Counterfeit banknote detection technology is a very major application research field, according to different detection methods and using different functions, it can enhance the detection efficiency of counterfeit banknote detection, which is a very major application field. Future scientific research will pay further attention to the development trend of this discipline and continue to innovate and optimise the detection technology to meet the needs of society for counterfeit currency detection technology.

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