# Research on an Even Number Which Minus 2 Can be Exactly Divided by 6 Can be Expressed as the Sum of Several Sets of Two Prime Numbers 

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#### Abstract

Using a 0 to $\mathrm{N}_{3}$ segment $\mathrm{X}_{\mathrm{B}}$ number axis to move two number axis units to the right and then overlap with a 0 to $\mathrm{N}_{3}$ segment $\mathrm{X}_{\mathrm{A}}$ number axis in the same direction, it's found that the overlapping number axis points of the two prime numbers are a set of twin prime numbers, and the law of twin prime numbers smaller than $\mathrm{N}_{3}$. Then, using the two $\mathrm{X}_{\mathrm{A}}$ number axes of the same length with them to overlapped in the opposite direction, it is found that the overlapping axis points of the twin primes are $\mathrm{P}(1,1)$, which is the twin primes of $\mathrm{N}_{3}$, which proves that $\mathrm{N}_{3}$ can also be expressed as the sum of several groups of two primes. Comparing the two overlapping number axes, it is found that the $\mathrm{X}_{\mathrm{A}} \backslash \mathrm{X}_{\mathrm{A}}{ }^{\prime}$ overlapping number axes are symmetrical, and it is found that prime numbers that make $6 \mathrm{~Pa}_{\mathrm{a}}$ exactly divide $\left(\mathrm{N}_{3}-2 \mathrm{P}_{\mathrm{a}}\right)$ or $6 \mathrm{P}_{\mathrm{b}}$ exactly divide $\left(\left(\mathrm{N}_{3}+2 \mathrm{P}_{\mathrm{b}}\right)\right.$ can also increase the table method number of $\mathrm{P}(1,1)$ prime pairs of $\mathrm{N}_{3}$, which proves that the number of $\mathrm{P}(1,1)$ primes of $\mathrm{N}_{3}$ to the table group is about equal to or more than half of the number of twin primes which is smaller than $\mathrm{N}_{3}$.


## 1. Introduction

By analyzing the smaller even numbers, it is found that except for 8 , the other even number which minus 2 can be exactly divided by 6 can be expressed as the sum of two $\mathrm{P}_{\mathrm{A}}=(6 \mathrm{~m}+1)$ primes, and the table method group count increases with the increase of even numbers, such as $14=(7+7)$, $26=(7+19)=(13+13), 50=(7+43)=(13+37)=(19+31)$. And the table method group count is also closely related to the number of groups of twin primes smaller than the even number.

The even number $\mathrm{N}_{3}\left(\mathrm{~N}_{3}=6 \mathrm{~m}+2, \mathrm{~m} \geq 2\right)$ is given. Except for 8 , the other even numbers which minus 2 can be exactly divided by 6 are in $\mathrm{N}_{3}$.

## 2. Characteristics of Twin Primes and Their Distribution on the Number Axis ${ }^{[1]}$

Except for 2 and 3, the composite numbers that cannot be exactly divided by 2 or 3 are all in the odd numbers of $A=6 \mathrm{~m}+1$ and $\mathrm{B}=6 \mathrm{~m}-1^{[2]}$. The prime numbers are represented by P , and the composite numbers are represented by $H$. If removes $H_{A}$ from $A$, the remaining is $\mathrm{P}_{\mathrm{A}}$; if removes $\mathrm{H}_{\mathrm{B}}$ from B , the remaining is $\mathrm{P}_{\mathrm{B}}$ (the prime number in this paper does not include 2 and 3 , and the composite number does not include the composite number that can be exactly divided by 2 or 3 ).

Make $\mathrm{X}_{\mathrm{A}}$ number axes that show only odd numbers A and $\mathrm{X}_{\mathrm{B}}$ number axes that show only odd numbers B. The parallel line of the vertical axis is made through the $\mathrm{N}_{3}$ point, and the 0 to $\mathrm{N}_{3}$ segments are intercepted respectively. Move the $X_{B}$ segment to the right by two units vertically up to overlap $\mathrm{X}_{\mathrm{A}}$, forming a twin prime overlapping number axes from 0 to $\mathrm{N}_{3}$ (LXAXB), where the B odd numbers all overlap with the A odd number, and the two primes form a twin prime overlapping number axes point.

Features of LXAXB:

1) The $X_{A}$ and $X_{B}$ axes overlap in the same direction.
2) The odd number A and B overlap to form (A, B) overlapping axis points, and the difference between the two numbers is 2 .
3) There are $\mathrm{N}_{3} / 6$ sets of (A, B) overlapping number axis points.
4) Frequency curves of the same wavelength neither intersect nor overlap.
5) The frequency curves of different wavelengths of the two number axes intersect at the overlapping number axis points, forming the LHH group with overlapping composite numbers $\left(\mathrm{H}_{\mathrm{A}}\right.$, $\mathrm{H}_{\mathrm{B}}$ ) of both Ep or Fp and Gp or Sp . The ( $\left.\# \mathrm{H}_{\mathrm{A}}-\mathrm{LHH}\right)$ group has only the $\left(\mathrm{H}_{\mathrm{A}}, \mathrm{P}_{\mathrm{B}}\right)$ overlapping number axis points of Ep or Fp , and the $\left(\# \mathrm{H}_{\mathrm{B}}-\mathrm{LHH}\right)$ group has only the $\left(\mathrm{H}_{\mathrm{B}}, \mathrm{P}_{\mathrm{A}}\right)$ overlapping number axis points of Gp or Sp . The remaining prime axis points overlap, forming $\mathrm{L}_{\mathrm{N} 3}$ groups of ( $\mathrm{P}_{\mathrm{A}}, \mathrm{P}_{\mathrm{B}}$ ) with no frequency curve, and the sum of the four overlapping axis points is equal to the total number of groups (A, B).

The number of groups of twin primes is obtained by using the residual relation:

$$
\begin{equation*}
\mathrm{L}_{\mathrm{N} 3}=\mathrm{N}_{3} / 6-\mathrm{LHH}-\left(\# \mathrm{H}_{\mathrm{A}}-\mathrm{LHH}\right)-\left(\# \mathrm{H}_{\mathrm{B}}-\mathrm{LHH}\right)=\mathrm{N}_{3} / 6+\mathrm{LHH}-\left(\# \mathrm{H}_{\mathrm{A}}+\# \mathrm{H}_{\mathrm{B}}\right) \tag{1}
\end{equation*}
$$

## 3. Characteristics of $\mathrm{N}_{3}$ Overlapping Number Axis are Analyzed by Overlapping Two $\mathbf{X}_{\mathrm{A}}$ Number Axes in the Opposite Direction

### 3.1 Make $\mathbf{X}_{\mathrm{A}} \mid \mathbf{X}_{\mathrm{A}}{ }^{\prime}$ Overlapping Number Axes

Take two $\mathrm{X}_{\mathrm{A}}$ from 0 to $\mathrm{N}_{3}$ and place them in the first and fourth quadrants of the planar rectangular coordinate system respectively.

The $\mathrm{X}_{\mathrm{A}}$ of the fourth quadrant is flipped $180^{\circ}$, the $\mathrm{N}_{3}$ point is on the Y axis, the direction is left, the Ep' is still above the number axis, and the $\mathrm{Fp}^{\prime}$ is still below the number axis, which is called $\mathrm{X}_{\mathrm{A}}{ }^{\prime}$ number axis. The $X_{A^{\prime}}$ after flipping is only opposite to the $X_{A}$, and other properties remain unchanged. $\mathrm{X}_{\mathrm{A}}{ }^{\prime}$ vertically moves up and overlaps with $\mathrm{X}_{\mathrm{A}}$ to form the $\mathrm{X}_{\mathrm{A}} \backslash \mathrm{X}_{\mathrm{A}^{\prime}}$ overlapping axis (XAXA) of $\mathrm{N}_{3}$. (Fig.1)

XAXA is equivalent to replacing Хв $_{\text {в }}$ LXAXB with $\mathrm{X}_{\mathrm{A}}$ and then flipping $180^{\circ}$, or replacing $X_{B}$ of $\mathrm{N}_{2}$ overlapping number axis XAXB ${ }^{[1]}$ with $\mathrm{X}_{A^{\prime}}$. Because $\mathrm{X}_{\mathrm{A}}$ and $\mathrm{X}_{\mathrm{B}}$ are the same in nature, its evaluation is the same as that of $\mathrm{N}_{2}$ overlapping number axis. On XAXA, the A' odd number of $\mathrm{X}_{\mathrm{A}}{ }^{\prime}$ all overlaps with the A odd number of $\mathrm{X}_{\mathrm{A}}$ (Except for the largest A and $\mathrm{A}^{\prime}$, which both overlap with the 1 of another number axis), and the two composite numbers overlap as ( $\mathrm{H}_{\mathrm{A}}, \mathrm{H}_{\mathrm{A}}{ }^{\prime}$ ) overlapping axis points. The two primes overlap as ( $\mathrm{P}_{\mathrm{A}}, \mathrm{P}_{\mathrm{A}}{ }^{\prime}$ ) overlapping number axis points, which are a set of $\mathrm{P}(1,1)$ prime pairs of $\mathrm{N}_{3}$. Although the $\mathrm{X}_{A^{\prime}}$ is in the opposite direction of $\mathrm{X}_{\mathrm{A}}$, the frequency curve is not directional, and the intersection rule of the frequency curve is not directional. Through the intersection rule of the frequency curve, the rule of $\left(\mathrm{H}_{\mathrm{A}}, \mathrm{H}_{\mathrm{A}}{ }^{\prime}\right)$ overlapping axis points is found, and the rule of $\mathrm{P}(1,1)$ prime pairs of $\mathrm{N}_{3}$ is found.


Figure 1: $\mathrm{X}_{\mathrm{A}} \backslash \mathrm{X}_{A^{\prime}}$ overlapping number axis $\left(\mathrm{N}_{3}=314\right)$ : $\mathrm{X}_{\mathrm{A}}$ and $\mathrm{X}_{\mathrm{A}}{ }^{\prime}$ are oppositely overlapped. The solid pentagram is $\left(\mathrm{H}_{\mathrm{A}}, \mathrm{H}_{\mathrm{A}^{\prime}}\right)$, the hollow pentagram is $\left(\mathrm{P}_{\mathrm{A}}, \mathrm{P}_{\mathrm{A}}{ }^{\prime}\right)$, the dot with horizontal line is $\left(\mathrm{H}_{\mathrm{A}}\right.$, $\left.\mathrm{P}_{\mathrm{A}}{ }^{\prime}\right)$, the dot with vertical line is $\left(\mathrm{H}_{\mathrm{A}^{\prime}}, \mathrm{P}_{\mathrm{A}}\right)$, and the heart shape is that the prime number 313 overlaps with1 of the other number axis and does not form ( $\mathrm{A}, \mathrm{A}^{\prime}$ )overlapping number axis points.

There are two cases of XAXA:

1) If $6 \mathrm{P}_{\mathrm{a}}$ can not exactly divide ( $\mathrm{N}_{3}-2 \mathrm{P}_{\mathrm{a}}$ ) nor can $6 \mathrm{P}_{\mathrm{b}}$ exactly divide $\left(\mathrm{N}_{3}+2 \mathrm{P}_{\mathrm{b}}\right)$, there will be no frequency curve overlap, which is called XAXA $_{1}$.
2) If $\left(\mathrm{N}_{3}-2 \mathrm{P}_{\mathrm{a}}\right)$ is divisible by $6 \mathrm{P}_{\mathrm{a}}$ or $\left(\mathrm{N}_{3}+2 \mathrm{P}_{\mathrm{b}}\right)$ is divisible by $6 \mathrm{P}_{\mathrm{b}}$, then there is a corresponding frequency curve overlap, called $\mathrm{XAXA}_{2}$.

### 3.2 Characteristics of the Overlapping Number Axis Points and the Group Count of XAXA $_{1}$

### 3.2.1 Characteristics of $\mathrm{XAXA}_{1}$



Figure 2: Pulling $\mathrm{X}_{\mathrm{A}^{\prime}}$ left and right can form any $\mathrm{X}_{\mathrm{A}} \backslash \mathrm{X}_{\mathrm{A}^{\prime}}$ overlapping number axis (when $\mathrm{N}_{3}=182$, $182-2 \times 7$ can be exactly divided by $6 \times 7$, and while a prime factor 7 exists, $7-\mathrm{Gp} / 7-\mathrm{Gp}$ ' is made overlapped)

1) Two identical $X_{A}$ overlap in the opposite directions.
2) Two $A$ odd numbers overlap to form ( $\mathrm{A}, \mathrm{A}^{\prime}$ ) overlapping number axis points, and the two numbers are complementary, and their sum is equal to $\mathrm{N}_{3}$.
3) There are ( $\mathrm{N}_{3} / 6-1$ ) sets of (A, $A^{\prime}$ ) overlapping number axis points, which is one set less than (A, B) of equal length LXAXB.
4) Frequency curves with the same wavelength neither intersect nor overlap.
5) The ( $\mathrm{P}_{\mathrm{A}}, \mathrm{P}_{\mathrm{A}}$ ) is evenly distributed on XAXA ${ }_{1}$.
3.2.2 The number of $\left(H_{A}, H_{A}{ }^{\prime}\right)$ overlapping composite group count of frequency curve intersection

The frequency curves of different wavelengths of the two axes will intersect on XAXA ${ }_{1}$ to form $\left(\mathrm{H}_{\mathrm{A}}, \mathrm{H}_{\mathrm{A}}{ }^{\prime}\right)$ overlapping number axis points with both Ep or Fp and Ep ' or Fp '. The group count of $\left(\mathrm{H}_{\mathrm{A}}, \mathrm{H}_{\mathrm{A}}{ }^{\prime}\right)$ is equal to the quotient obtained by dividing the length of the overlapping number axis by 6 times the product of the wavelength roots of the relevant frequency curve.

The Ep\Gp intersection ${ }^{[1]}$ of LXAXB is the same as the Ep\Ep' intersection of XAXA 1 . Ep and $E p^{\prime}$ with the same wavelength neither intersect nor overlap, but Ep and other Ep' do intersect. One or more Ep will also intersect with one or more Ep' at the same overlapping number axes point, with $\sum_{\text {ee }}$ comprehensively representing the Ep\Ep' intersection ( $\mathrm{H}_{\mathrm{A}}, \mathrm{H}_{\mathrm{A}}{ }^{\prime}$ ) group count.

The $\mathrm{Ep} \backslash \mathrm{Sp}$ intersection ${ }^{[1]}$ of LXAXB is the same as the $\mathrm{Ep} \backslash \mathrm{Fp}^{\prime}$ intersection of XAXA 1 . Both Ep and $\mathrm{Fp}^{\prime}$ intersect, and one or more Ep will also intersect with one or more $\mathrm{Fp}^{\prime}$ at the same overlapping number axes point, and the group count of ( $\mathrm{H}_{\mathrm{A}}, \mathrm{H}_{\mathrm{A}}{ }^{\prime}$ ) where Ep\Fp' intersects is represented by $\sum_{\text {ef }}$.

The Fp\Gp intersection ${ }^{[1]}$ of LXAXB is the same as the Fp\Ep' intersection of XAXA 1. Fp and $E p^{\prime}$ intersect with each other, and one or more Fp will also intersect with one or more Ep' at the same overlapping number axis point. The group count of ( $\mathrm{H}_{\mathrm{A}}, \mathrm{H}_{\mathrm{A}}{ }^{\prime}$ ) where $\mathrm{Fp} \backslash E p^{\prime}$ intersects is represented by $\sum_{\mathrm{ff}^{\prime}}$.

The Fp\Sp intersection ${ }^{[1]}$ of LXAXB is the same as the $\mathrm{Fp} \backslash \mathrm{Fp}$ ' intersection of XAXA 1. Fp and $\mathrm{Fp}^{\prime}$ with the same wavelength neither intersect nor overlap, but Fp and other $\mathrm{Fp}^{\prime}$ do intersect. One or more Fp will also intersect with one or more $\mathrm{Fp}^{\prime}$ at the same overlapping number axes point, with $\sum_{\mathrm{ff}} \mathrm{comprehensively}$ representing the $\mathrm{Fp} \backslash \mathrm{Fp}$ ' intersection $\left(\mathrm{H}_{\mathrm{A}}, \mathrm{H}_{\mathrm{A}^{\prime}}\right)$ group count.

Same as the intersection of multiple frequency curves ${ }^{[1]}$ of LXAXB, the two frequency curves can also intersect at the same point with the third frequency curve, and the three frequency curves can also intersect at the same point with the fourth frequency curve. The intersection of multiple frequency curves takes up more frequency curve axis points, which reduces the group count of $\left(\mathrm{H}_{\mathrm{A}}\right.$, $\mathrm{H}_{\mathrm{A}}{ }^{\prime}$ ) counted by the intersection of the two frequency curves, and such reduced group count is represented by $\sum$ efe'f'.
$\mathrm{N}_{3} \mathrm{HH}$ is used to represent the group count of all $\left(\mathrm{H}_{\mathrm{A}}, \mathrm{H}_{\mathrm{A}}{ }^{\prime}\right)$ overlapping number axis points: $\mathrm{N}_{3} \mathrm{HH}=\sum_{\mathrm{ee}^{\prime}+}+\mathrm{eff}^{\prime}+\sum \mathrm{fe}^{\prime}+\sum \mathrm{ffr}^{\prime}-\sum \mathrm{efe}^{\prime} \mathrm{f}^{\prime} \mathrm{f}^{\prime}$

It is the same as the LHH calculation formula ${ }^{[1]}$ of the group count of overlapping composite of LXAXB, and the number is basically equal.

### 3.2.3 The group count of $(\mathbf{H}, \mathrm{P})$ overlapping number axis points of the frequency curve with only one number axis

$\mathrm{X}_{\mathrm{A}}$ has $\# \mathrm{H}_{\mathrm{A}} \mathrm{H}_{\mathrm{A}}$. Except for the $\mathrm{N}_{3} \mathrm{HH}$ groups of $\left(\mathrm{H}_{\mathrm{A}}, \mathrm{H}_{A^{\prime}}\right)$ composed of $\mathrm{H}_{\mathrm{A}}$ and $\mathrm{H}_{A^{\prime}}$, the remaining $\mathrm{H}_{\mathrm{A}}$ overlaps with $\mathrm{P}_{A^{\prime}}$ to form the $\left(\# \mathrm{H}_{\mathrm{A}}-\mathrm{N}_{3} \mathrm{HH}\right)$ groups of overlapping number line points with only Ep or $\mathrm{Fp}\left(\mathrm{H}_{\mathrm{A}}, \mathrm{P}_{\mathrm{A}^{\prime}}\right)$.
$\mathrm{X}_{\mathrm{A}}$ has $\# \mathrm{H}_{\mathrm{A}} \mathrm{H}_{\mathrm{A}^{\prime}}$. Except for the $\mathrm{N}_{3} \mathrm{HH}$ groups of ( $\mathrm{H}_{\mathrm{A}}, \mathrm{H}_{\mathrm{A}^{\prime}}$ ) composed of $\mathrm{H}_{\mathrm{A}}$ and $\mathrm{H}_{\mathrm{A}^{\prime}}$, the remaining $\mathrm{H}_{\mathrm{A}^{\prime}}$ overlaps with $\mathrm{P}_{\mathrm{A}}$ to form the ( $\# \mathrm{H}_{\mathrm{A}^{\prime}}-\mathrm{N}_{3} \mathrm{HH}$ ) groups of overlapping number line points with only $\mathrm{Ep}^{\prime}$ or $\mathrm{Fp}^{\prime}\left(\mathrm{H}_{\mathrm{A}^{\prime}}, \mathrm{P}_{\mathrm{A}}\right)$.

### 3.2.4 The group count of $\left(\mathrm{P}_{\mathrm{A}}, \mathrm{P}_{\mathrm{A}}{ }^{\prime}\right)$ overlapping axis points without frequency curve

The remaining prime axis points overlap to form ( $\mathrm{P} \mathrm{A}, \mathrm{P}_{\mathrm{A}}$ ) overlapping axis points without frequency curve. The sum of the four overlapping axis points is equal to the total group count of ( A , $\mathrm{A}^{\prime}$ ) overlapping axis points.

The group count of $\left(\mathrm{P}_{\mathrm{A}}, \mathrm{P}_{\mathrm{A}}{ }^{\prime}\right)$ overlapping number axes points is obtained by using the residual
relation:

$$
\begin{equation*}
\mathrm{d}=\left(\mathrm{N}_{3} / 6-1\right)-\mathrm{N}_{3} \mathrm{HH}-2\left(\# \mathrm{H}_{\mathrm{A}}-\mathrm{N}_{3} \mathrm{HH}\right)=\left(\mathrm{N}_{3} / 6-1\right)+\mathrm{N}_{3} \mathrm{HH}-2 \# \mathrm{H}_{\mathrm{A}} \tag{2}
\end{equation*}
$$

It is known that the number of composite axis points of $X_{A}$ and $X_{B}$ with equal length is basically equal ${ }^{[2]}$, so $2 \# H_{A}$ and $\left(\# H_{A}+\# H_{B}\right)$ is basically equal. There are $\left(N_{3} / 6-1\right)$ groups of (A, $\left.A^{\prime}\right)$ overlapping axis points in XAXA $_{1}$, which is one group less than the (A, B) overlapping axis points of LXAXB with equal length, and the larger even number is ignored, so the group count of $d$ and $\mathrm{L}_{\mathrm{N}} 3$ is basically equal.

### 3.2.5 Symmetry of XAXA $_{1}$

If the axis points $\mathrm{A}_{1}$ of $\mathrm{X}_{\mathrm{A}}$ and $\left(\mathrm{N}_{3}-\mathrm{A}_{1}\right)^{\prime}$ of $\mathrm{XA}^{\prime}$ overlap, then $\left(\mathrm{N}_{3}-\mathrm{A}_{1}\right)$ of $\mathrm{X}_{\mathrm{A}}$ must overlap with the complementary $\mathrm{A}_{1}$ ' of $\mathrm{XA}^{\prime}$. Although there are two different sets of overlapping axis points on $\mathrm{XAXA}_{1}$, their odd pairs are the same. The distance between one set of overlapping axis points and the origin of $\mathrm{X}_{\mathrm{A}}$ is equal to the distance between the other set of overlapping axis points and the origin of $\mathrm{XA}^{\prime}$, that is, they are symmetrical for the midpoint of XAXA ${ }_{1}$ (Fig. 1 and Fig.2).

If ( $\mathrm{N}_{3} / 6-1$ ) is an even number, the midpoint of $\mathrm{XAXA}_{1}$ is not on the ( $\mathrm{A}, \mathrm{A}^{\prime}$ ) overlapping axis points, and the axis points on both sides of the midpoint are symmetrical, then there are $\left(\mathrm{N}_{3} / 6-1\right) \div 2$ sets of ( $A, A^{\prime}$ ) odd pairs. If $\left(N_{3} / 6-1\right)$ is an odd number, the midpoint of $X_{A X A}$ is a set of the same A , and the remaining points of the overlapping number axes are symmetric with each other, then there are $\mathrm{N}_{3} / 12$ groups of ( $\mathrm{A}, \mathrm{A}^{\prime}$ ) odd pairs, and this difference is ignored when $\mathrm{N}_{3}$ is larger.

Therefore, the group count of the composite pairs corresponding to ( $\mathrm{H}_{\mathrm{A}}, \mathrm{H}_{\mathrm{A}^{\prime}}$ ) on XAXA ${ }_{1}$ is equal to half of the group count of $\left(\mathrm{H}_{\mathrm{A}}, \mathrm{H}_{\mathrm{A}}{ }^{\prime}\right)$ overlapping axis points $\mathrm{N}_{3} \mathrm{HH}$, and the group count of $\mathrm{P}(1,1)$ prime pairs corresponding to ( $\mathrm{P}_{\mathrm{A}}, \mathrm{P}_{\mathrm{A}}{ }^{\prime}$ ) overlapping axis points $\mathrm{D}_{\mathrm{N}}$ is equal to half of the group count of ( $\mathrm{P}_{\mathrm{A}}, \mathrm{P}_{\mathrm{A}}$ ) overlapping axis points d .

### 3.2.6 The similarities and differences between $\mathrm{XAXA}_{1}$ and LXAXB

### 3.2.6.1 The similarities

1) XAXA $_{1}$ has ( $\mathrm{N}_{3} / 6-1$ ) groups of ( $\mathrm{A}, \mathrm{A}^{\prime}$ ), which is one group less than group (A, B) of equal length LXAXB. For larger $\mathrm{N}_{3}$, the difference of the total number of groups of overlapping number axis points is ignored, so the total number of groups is basically equal.
2) The rule of frequency curve intersection is consistent.
3) Frequency curves with the same wavelength neither intersect nor overlap.
4) The group count of $\mathrm{N}_{3} \mathrm{HH}$ and LHH is basically equal.
5) The group count of $\left(\mathrm{P}_{\mathrm{A}}, \mathrm{P}_{\mathrm{A}}{ }^{\prime}\right)$ overlapping axis points d is basically equal to that of $\left(\mathrm{P}_{\mathrm{A}}, \mathrm{P}_{\mathrm{B}}\right)$ overlapping axis points $\mathrm{L}_{\mathrm{N} 3}$.

### 3.2.6.2 The differences

1) XAXA $_{1}$ is composed of two $X_{A}$ with opposite directions. LXAXB is composed of one $X_{A}$ and one $\mathrm{X}_{\mathrm{B}}$, and the directions of the two axes are the same.
2) $\mathrm{XAXA}_{1}$ overlapping axis points are two A odd numbers, two numbers are complementary, and their sum is equal to $\mathrm{N}_{3}$; the overlapping axis points of LXAXB are one A and one B , and the difference between the two numbers is 2 .
3) $\mathrm{XAXA}_{1}$ is symmetrical for the midpoint; LXAXB has no symmetry.
4) The $\left(\mathrm{P}_{\mathrm{A}}, \mathrm{P}_{\mathrm{A}}{ }^{\prime}\right)$ overlapping axis points are evenly distributed on $\mathrm{XAXA}_{1}$. The ( $\mathrm{P}_{\mathrm{A}}, \mathrm{P}_{\mathrm{B}}$ ) overlapping axis points are dense first and then sparse on LXAXB.
5) The $P(1,1)$ prime pair group count $D_{N 3}$ of $N_{3}$ is equal to half of the group count $d$ of the $\left(\mathrm{P}_{\mathrm{A}}\right.$,
$\mathrm{P}_{A^{\prime}}$ ) overlapping axis points of $\mathrm{XAXA}_{1}$. The group count of twin primes $\mathrm{L}_{\mathrm{N} 3}$ which is smaller than $\mathrm{N}_{3}$ is equal to the group count of $\left(\mathrm{P}_{\mathrm{A}}, \mathrm{P}_{\mathrm{B}}\right)$ overlapping axis points of LXAXB.

### 3.2.7 Variance analysis

According to the comparison between randomly selected XAXA ${ }_{1}$ and LXAXB of equal length, the group count of $\mathrm{P}(1,1)$ prime pairs of XAXA 1 is slightly less than half of the group count of twin prime pairs of LXAXB of equal length.

From the analysis of the residual relationship, for the even number of $\mathrm{N}_{3}, \# \mathrm{H}_{\mathrm{A}}$ is fixed, only the change of the group count of $\left(\mathrm{H}_{\mathrm{A}}, \mathrm{H}_{\mathrm{A}}{ }^{\prime}\right)$ will affect the group count of $\left(\mathrm{P}_{\mathrm{A}}, \mathrm{P}_{\mathrm{A}}{ }^{\prime}\right)$.

### 3.2.7.1 The intersection of non-composite number dash lines of a frequency curve

Ep extends to the left side of the Y axis with a dash line, and has a dash line intersection with $\mathrm{X}_{\mathrm{A}}$, which is the non-composite number dash line intersection of the frequency curve. It is the prime number of the wavelength root itself, and the non-composite dash line intersection of Ep is at the left end. Fp has no dash line intersection.
$\mathrm{X}_{\mathrm{A}}$ flips $180^{\circ}$ to become $\mathrm{X}_{\mathrm{A}}{ }^{\prime}$, and the dash line intersection of Ep' moves to the right.

### 3.2.7.2 The influence of the intersection point of non-composite dash line on $\left(\mathrm{H}_{\mathrm{A}}, \mathrm{H}_{\mathrm{A}}{ }^{\prime}\right)$

The number axis segment from 0 to the intersection of non-composite dash lines is the noncomposite segment $(\mathrm{NOH})$ of the frequency curve. Remove NOH , the remaining number axis segment is the segment where the frequency curve intersects with other frequency curves. The exact group conut of $\left(\mathrm{H}_{\mathrm{A}}, \mathrm{H}_{\mathrm{A}}{ }^{\prime}\right)$ is obtained by dividing the length of the intersection area by 6 times the product of the wavelength roots of the correlated frequency curve.

Both Ep and Sp have NOH , and the NOH of Ep and Sp on LXAXB is at the left end. The intersection of EplSp: The two NOH overlap and the intersection area only remove the larger wavelength NOH .

The intersection of Ep\Ep': remove the NOH of the left end Ep, and then remove the NOH of the right end Ep'. Compared with the Ep\Sp intersection area with both NOH of LXAXB, the smaller wavelength NOH is removed, which shortens the intersection area and may reduce one group $\left(\mathrm{H}_{\mathrm{A}}\right.$, $\mathrm{HA}^{\prime}$ '). The larger the even number, the more the frequency curve; the more the intersection of $\mathrm{Ep} \backslash \mathrm{Ep}$ ', and the more the chance of reducing one group ( $\mathrm{H}_{\mathrm{A}}, \mathrm{H}_{\mathrm{A}}{ }^{\prime}$ ), but the proportion of reduced groups in the whole $\mathrm{N}_{3} \mathrm{HH}$ is very small. According to the group count of all $\mathrm{Ep} \backslash E p^{\prime}$ intersection, the area of the curved trapezoid is counted. The curved trapezoid is composed of (\#Ep-1)x\#Ep vertical lines representing Ep $\backslash E p^{\prime}$ intersection. Each vertical line is composed of $\mathrm{N}_{3} /\left(6 \mathrm{P}_{\mathrm{a}} * \mathrm{P}_{\mathrm{a}}{ }^{\prime}\right)$ points representing the group count of $\left(\mathrm{H}_{\mathrm{A}}, \mathrm{H}_{A^{\prime}}\right)$. The denominator of the reduced group count in the proportion of $\mathrm{N}_{3} \mathrm{HH}$ is the area of the curved trapezoid, and the numerator is half the length of the curved edge (calculated as equal as or less than half of the group count of each vertical line $\left(\mathrm{H}_{\mathrm{A}}, \mathrm{H}_{\mathrm{A}^{\prime}}\right)$ ), so the proportion of $\left(\mathrm{H}_{\mathrm{A}}, \mathrm{H}_{\mathrm{A}}{ }^{\prime}\right)$ reduction is very small.

### 3.2.7.3 Influence of intersection starting point on $\left(\mathrm{H}_{\mathrm{A}}, \mathrm{H}_{\mathrm{A}}{ }^{\prime}\right)$

Fp\Fp' has no NOH, Ep\Fp', Fp\Ep' has only one NOH, and these three kinds of intersections have not shortened the intersection area because of $\mathrm{X}_{\mathrm{A}}$ flipping $180^{\circ}$. However, compared with the LXAXB overlap axis, there are also differences in the length of the intersection area due to different starting points, resulting in differences between the group count of $\left(\mathrm{H}_{\mathrm{A}}, \mathrm{H}_{A^{\prime}}\right)$ and $\left(\mathrm{H}_{\mathrm{A}}, \mathrm{H}_{\mathrm{B}}\right)$.


Figure 3: There is no significant difference between $\mathrm{D}_{\mathrm{N} 3}$ and $\mathrm{L}_{\mathrm{N} 3} / 2$ for even number $\mathrm{N}_{3}$ which is without prime factors

The intersection starting point of two frequency curves on LXAXB is fixed, such as 145, the intersection starting point of $5-\mathrm{Fp} \backslash 11-\mathrm{Sp}$ (abscissa); 121, the intersection starting point of $11-\mathrm{Fp} \backslash 17-$ Sp. The intersection starting point of $\mathrm{XAXA}_{1}$ is related to $\mathrm{N}_{3}$. When $\mathrm{N}_{3}$ is equal to 1004,10004 and 100004 , the intersection starting point of $5-\mathrm{Fp} \backslash 11-\mathrm{Fp}$ ' is 25,115 and 25 , and the intersection starting point of $11-\mathrm{Fp} \backslash 17-\mathrm{Fp}$ ' is 715,1045 and 979 . The intersection area is slightly longer when the starting point of the intersection is small, and the intersection area is slightly shorter when the starting point of the intersection is large, which may make the $\left(\mathrm{H}_{\mathrm{B}}, \mathrm{H}_{\mathrm{B}}{ }^{\prime}\right)$ of XAXA ${ }_{1}$ less than 1 group or more than 1 group of $\left(\mathrm{H}_{\mathrm{A}}, \mathrm{H}_{\mathrm{B}}\right)$ of LXAXB. The smaller even number will affect the ratio of the table method group count to the group count of twin prime, but the differences caused by different starting points are partially offset by the intersection of many frequency curves and the intersection of multiple frequency curves. Although the number of differences is not small, it has an impact on the group count of overlapping composite number, but it has little effect on the ratio of the group count of twin prime.

Due to the combined effect of these factors, the overlapping composite number of XAXA $_{1}$ is slightly less than that of LXAXB, so $\left(\mathrm{P}_{\mathrm{A}}, \mathrm{P}_{\mathrm{A}}{ }^{\prime}\right)$ is reduced, but the proportion of reduction is very small. According to the comparison between randomly selected XAXA ${ }_{1}$ and isometric LXAXB, the average group count of $\mathrm{P}(1,1)$ prime pairs of $\mathrm{XAXA}_{1}$ is about $1.2 \%$ less than half of the group count of twin prime pairs of LXAXB, but not up to $5 \%$. According to statistical regulations, there is no significant difference (Fig. 3).

Therefore, the group count of $\mathrm{P}(1,1)$ prime pairs corresponding to $\left(\mathrm{P}_{\mathrm{A}}, \mathrm{PA}^{\prime}\right)$ of $\mathrm{XAXA}_{1}$ is about half of the group count of twin prime pairs smaller than $\mathrm{N}_{3}$ : $\mathrm{D}_{\mathrm{N} 3} \approx 0.5 \mathrm{~L}_{\mathrm{N} 3}$

If ( $\mathrm{N}_{3}-3$ ) is a prime number, the $\mathrm{N}_{3}$ can also be expressed as ( $\mathrm{P}_{\mathrm{B}}+3$ ) prime pairs (In the figure, $\mathrm{w}=1$ indicates that the even number has the $\mathrm{N}_{3}=\left(\mathrm{P}_{\mathrm{B}}+3\right)$ table method, but the group count can be ignored.)

### 3.3 Characteristics of the overlapping number axis points and the group count of XAXA ${ }_{2}$

On XAXA $_{1}$, the frequency curves with the same wavelength do not intersect or overlap, but intersect with other frequency curves. The unintersected number axis points overlap with the prime number axis points of another number axis, forming $\left(\mathrm{H}_{\mathrm{A}}{ }^{\prime}, \mathrm{P}_{\mathrm{A}}\right)$ and $\left(\mathrm{H}_{\mathrm{A}}, \mathrm{P}_{\mathrm{A}}{ }^{\prime}\right)$ overlapping number axis points.

On XAXA 2 , if $\left(\mathrm{N}_{3}-2 \mathrm{P}_{\mathrm{a}}\right)$ can be exactly divided by $6 \mathrm{P}_{\mathrm{a}}$, then the Ep with $\mathrm{P}_{\mathrm{a}}$ as the wavelength root completely overlaps with the $\mathrm{Ep}^{\prime}$ with the same wavelength (Fig.2), and the total number of
composite number axis points $\left(\mathrm{H}_{\mathrm{A}}, \mathrm{H}_{\mathrm{A}^{\prime}}\right)$, then $\left(\mathrm{H}_{\mathrm{A}}, \mathrm{H}_{\mathrm{A}^{\prime}}\right)$ increases. At the same time, the overlap with the other number axis primes is reduced, so that ( $\mathrm{P}_{\mathrm{A}}, \mathrm{P}_{\mathrm{A}}{ }^{\prime}$ ) increases. The increased group count is about $\left(\mathrm{L}_{\mathrm{N} 3} \times 0.494 \times\left(1+3 \div \mathrm{P}_{\mathrm{a}}\right) \div \mathrm{P}_{\mathrm{a}}\right)$, which means this increased group count is about $1 / \mathrm{P}_{\mathrm{a}}$ of half group count of twin prime (Figure 4). And every $\left(\mathrm{P}_{\mathrm{a}}-1\right) \mathrm{N}_{3}$, there is a $\mathrm{N}_{3}$ that can be exactly divided by the $\left(6 \mathrm{P}_{\mathrm{a}}\right)$, so that $\left(\mathrm{P}_{\mathrm{A}}, \mathrm{P}_{\mathrm{A}}{ }^{\prime}\right)$ increases.

Similarly, if $\left(\mathrm{N}_{3}+2 \mathrm{P}_{\mathrm{b}}\right)$ can be exactly divided by $6 \mathrm{P}_{\mathrm{b}}$, then the Fp of the $\mathrm{P}_{\mathrm{b}}$ for the wavelength root completely overlaps with the Fp with the same wavelength root, which reduces the overlap with the prime number of the other number axis, and increases the ( $\mathrm{P}_{\mathrm{A}}, \mathrm{P}_{\mathrm{A}}{ }^{\prime}$ ). And every $\left(\mathrm{P}_{\mathrm{A}}-1\right) \mathrm{N}_{3}$, there is a $\mathrm{N}_{3}$ that can be exactly divided by the $\left(6 \mathrm{P}_{\mathrm{b}}\right)$, so that $\left(\mathrm{P}_{\mathrm{A}}, \mathrm{P}_{\mathrm{A}^{\prime}}\right)$ increases. These primes that make $6 \mathrm{P}_{\mathrm{a}}$ exactly divide $\left(\mathrm{N}_{3}-2 \mathrm{P}_{\mathrm{a}}\right)$ or $6 \mathrm{P}_{\mathrm{b}}$ exactly divide $\left(\mathrm{N}_{3}+2 \mathrm{P}_{\mathrm{b}}\right)$ and increase $\left(\mathrm{P}_{\mathrm{A}}, \mathrm{P}_{\mathrm{A}}\right.$ ) are called prime factors of the even number.

If multiple $\mathrm{P}_{\mathrm{a}}$ can make $6 \mathrm{P}_{\mathrm{a}}$ exactly divide ( $\mathrm{N}_{3}-2 \mathrm{P}_{\mathrm{a}}$ ) or multiple $\mathrm{P}_{\mathrm{b}}$ can make $6 \mathrm{P}_{\mathrm{b}}$ exactly divide $\left(\left(\mathrm{N}_{3}+2 \mathrm{P}_{\mathrm{b}}\right)\right.$, or both $\mathrm{P}_{\mathrm{a}}$ and $\mathrm{P}_{\mathrm{b}}$ can make $6 \mathrm{P}_{\mathrm{a}}$ exactly divide $\left(\mathrm{N}_{3}-2 \mathrm{P}_{\mathrm{a}}\right)$, and $6 \mathrm{P}_{\mathrm{b}}$ exactly divide $\left(\mathrm{N}_{3}+2 \mathrm{P}_{\mathrm{b}}\right)$, then $\left(\mathrm{P}_{\mathrm{A}}, \mathrm{P}_{\mathrm{A}}{ }^{\prime}\right)$ is affected by these prime factors.


Figure 4: The influence of prime factors on continuous $\mathrm{N}_{3}$ even number $\mathrm{D}_{\mathrm{N}}$
The increase of $\left(\mathrm{P}_{\mathrm{A}}, \mathrm{P}_{\mathrm{A}}{ }^{\prime}\right)$ is inversely proportional to the size of the prime factor. The smaller the prime factor, the more $\left(\mathrm{P}_{\mathrm{A}}, \mathrm{P}_{\mathrm{A}}{ }^{\prime}\right)$ increases. It is also related to the number of prime factors. The more prime factors, the more ( $\mathrm{P}_{\mathrm{A}}, \mathrm{P}_{\mathrm{A}}{ }^{\prime}$ ) increase (Fig.4). However, the prime factor does not change the symmetry of the overlapping number axis. And due to symmetry, the increased $\mathrm{P}(1,1)$ prime pairs are only half of the increased $\left(\mathrm{P}_{\mathrm{A}}, \mathrm{P}_{\mathrm{A}}{ }^{\prime}\right)$ overlapping axis points.

Therefore, the group count of ( $\mathrm{P}_{\mathrm{A}}, \mathrm{PA}^{\prime}$ ) overlapping axis points of XAXA is approximately equal to or more than the group count of $\left(\mathrm{P}_{\mathrm{A}}, \mathrm{P}_{\mathrm{B}}\right)$ overlapping axis points of LXAXB, and the group count of $\mathrm{P}(1,1)$ prime pairs corresponding to $\left(\mathrm{P}_{\mathrm{A}}, \mathrm{P}_{\mathrm{A}}{ }^{\prime}\right)$ is approximately equal to or more than half of the group count of twin prime pairs: $\mathrm{D}_{\mathrm{N} 3} \geq 0.5 \mathrm{~L}_{\mathrm{N} 3}$.

### 3.4 The Group Count of $\mathbf{P}(1,1)$ Prime Pair of Infinity $\mathbf{N}_{3}$

$P_{A}$ is infinite ${ }^{[2]}$. When $N_{3}$ increases to $\left(2 N_{3}-2\right)$, there will be no $P_{A}$ from 0 to $N_{3}$ number axis and no $P_{A}$ from $\mathrm{N}_{3}$ to ( $2 \mathrm{~N}_{3}-2$ ) number axis, and the intersection rule of frequency curve remains unchanged. Therefore, $\mathrm{N}_{3}$ doubling still follows the rule of $\mathrm{D}_{\mathrm{N} 3} \geq 0.5 \mathrm{~L}_{\mathrm{N}}$. $\mathrm{N}_{3}$ infinitely doubles, and these properties will not change. At present, although it is not certain that the group count of twin prime is infinite; the known number of twin primes will not disappear. The group count of $\mathrm{P}(1,1)$ prime pairs of infinite $\mathrm{N}_{3}$ must be more than half of the known group count of twin prime.

### 3.5 Group Count of $\mathbf{P}(1,1)$ Prime Pairs of Continuous $\mathbf{N}_{3}$ Even Number

In the planar rectangular coordinate system, a parabola ( $\mathrm{L}_{\mathrm{N} 3} / 2$ curve) is formed by connecting the points with $\mathrm{N}_{3}$ as the abscissa and $0.5 \mathrm{~L}_{\mathrm{N}}$ as the vertical coordinate, which is half of the group count of twin prime smaller than $\mathrm{N}_{3}$. Then connect the points with $\mathrm{N}_{3}$ as the abscissa and the $\mathrm{P}(1,1)$ prime pair of $\mathrm{N}_{3}$ as the vertical coordinate to the group count $\mathrm{D}_{\mathrm{N} 3}$ ( $\mathrm{D}_{\mathrm{N} 3}$ connection). The influence of the prime factor makes the $\mathrm{D}_{\mathrm{N} 3}$ of the adjacent $\mathrm{N}_{3}$ vary greatly, and the standard curve cannot be formed. The above of the connection line is uneven and irregular, like a crocodile tail. With the increase of the even number, the shape is like a hand-painted porcupine back, and the many lowest points below the connection line (the ( $\mathrm{P}_{\mathrm{A}}, \mathrm{P}_{\mathrm{A}}{ }^{\prime}$ ) group count of $\mathrm{XAXA}_{1}$ is the point of the vertical coordinate) form a smooth curve, which is basically consistent with the $\mathrm{L}_{\mathrm{N}} / 2$ curve. The connection line does not break through the $\mathrm{L}_{\mathrm{N}} / 2$ curve downward (basically) no matter how it fluctuates. The overall trend of the connection increases with the increase of $\mathrm{N}_{3}$ (Fig.4).

## 4. Conclusion

The even number 8 can be expressed as the sum of $(3+5)$, and the other even number which minus 2 can be exactly divided by 6 can be expressed as the sum of two $\mathrm{P}_{\mathrm{A}}$. The table method group count is approximately equal to or more than half of the group count of twin prime smaller than the even number.

## References

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